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# Choosing Sampling Rates for Robot Control

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## Abstract

In our previous research, we experimentally implemented and evaluated the effect of dynamics compensation in model-based control algorithms. In this paper, we evaluate the effect of changing the control sampling period on the performance of the computed-torque and independent joint control schemes. While the former utilizes the complete dynamics model of the manipulator, the latter assumes a decoupled and linear model of the manipulator dynamics. We discuss the design of controller gains for both the computed-torque and the independent joint control schemes and establish a framework for comparing their trajectory tracking performance. Our experiments show that within each scheme the trajectory tracking accuracy varies slightly with the change of the sampling rate. However, at low sampling rates the computed-torque scheme outperforms the independent joint control scheme. Based on our experimental results, we also conclusively establish the importance of high sampling rates as they result in an increased stiffness of the system.

## 1. Introduction

Although many simulation results have been presented [13, 12, 4], the real-time implementation and performance of model-based control schemes with high control sampling rates had not been demonstrated on actual manipulators, until recently [9, 11, 1]. The main reasons for this have been the lack of a suitable manipulator system, that it is difficult to evaluate the dynamics parameters for implementing model-based algorithms. One of the goals of the CMU Direct-Drive Arm II [14] project has been to overcome these difficulties and evaluate the effect of dynamics compensation on the real-time trajectory tracking of manipulators. For the real-time computation of the inverse dynamics, we have developed a high-speed and powerful computational environment. The computation of inverse dynamics has been customized for the CMU DD Arm II and a computation time of 1 *ms* has been achieved [5]. To obtain an accurate model we have computed and measured the various parameters from the engineering drawings of the CMU DD Arm II by modeling each link as a composite of hollow and solid cylinders, prisms, and rectangular parallelepipeds. We have also proposed an algorithm to identify the dynamics parameters [8] which has been implemented on the CMU DD Arm II. The results of the experimental implementation of our identification algorithm are presented [6, 7]. Finally, the negligible friction in our direct-drive arm especially makes it suitable to test the efficacy of the computed-torque scheme.

In our previous research, we investigated the effect of high sampling rate dynamics compensation in model-based manipulator control methods. Specifically, we compared the computed-torque scheme which utilizes the complete dynamics model of the manipulator with the independent joint control scheme [9] and the feedforward compensation method [10]. The control schemes were implemented on the CMU DD Arm II with a sampling period of 2 *ms*. In this paper, we investigate the effect of reducing the sampling rate on the trajectory tracking performance of manipulator control methods. We first compare the performance of each scheme as the sampling rate is changed. Next, we also compare the relative performance of both the computed-torque and the independent joint control schemes at different **sampling rates**.

This paper is organized as follows: In Section 2, we present an overview of the manipulator control schemes that have been implemented and evaluated on the CMU DD Arm II. The design of controllers is discussed in Section 3 and the real-time experimental results are presented and interpreted in Section 4. Finally, in Section 5 we summarize this paper. In the Appendix, we describe our experimental hardware set-up.

## 2. Manipulator Control Techniques

The robot control problem revolves around the computation of the actuating joint torques/forces to follow the desired trajectory. The dynamics of a manipulator are described by a set of highly nonlinear and coupled differential equations. The complete dynamic model of an *N*-degrees-of-freedom manipulator is described by:

$$\tau = \mathbf{D}(\theta)\ddot{\theta} + h(\theta, \dot{\theta}) + g(\theta) \quad (1)$$

where  $\tau$  is the  $N$ -vector of the actuating torques;  $D(\theta)$  is the  $N \times N$  position dependent manipulator inertia matrix;  $h(\theta, \dot{\theta})$  is the  $N$ -vector of Coriolis and centrifugal torques;  $g(\theta)$  is the  $N$ -vector of gravitational torques; and  $\ddot{\theta}$ ,  $\dot{\theta}$  and  $\theta$  are  $N$ -vectors of the joint accelerations, velocities and positions, respectively.

This complex description of the system makes the design of controllers a difficult task. To circumvent the difficulties the control engineer often assumes a simplified model to proceed with the controller design. Industrial manipulators are usually controlled by conventional PID-type independent joint control structures designed under the assumption that the dynamics of the links are uncoupled and linear. The controllers based on such an overly simplified dynamics model result in low speeds of operation and overshoot of the end-effector.

To establish a framework for comparing the performance these two schemes, we consider the control law in two steps; computation of the commanded acceleration and computation of the control torque. The commanded joint accelerations  $u_i$  can be computed in one of the following three ways:

$$u_1 = K_p(\theta_d - \theta) - K_v\dot{\theta} \quad (2)$$

$$u_2 = K_p(\theta_d - \theta) + K_v(\dot{\theta}_d - \dot{\theta}) \quad (3)$$

$$u_3 = K_p(\theta_d - \theta) + K_v(\dot{\theta}_d - \dot{\theta}) + \ddot{\theta}_d \quad (4)$$

where  $K_p$  and  $K_v$  are  $N \times N$  diagonal position and velocity gain matrices, respectively. The  $N$ -vectors  $\theta_d$  and  $\theta$  are the desired and measured joint positions, respectively, and the " . " indicates the time derivative of the variables. Whereas only the position error and the velocity damping is used in equation (2), the commanded acceleration signal in equation (3) uses a velocity feedforward term, and the commanded acceleration signal in equation (4) uses both the velocity and acceleration feedforward terms. The idea is to increase the speed of response by incorporating a feedforward term.

The fundamental difference between the independent joint control schemes and the model-based schemes lies in the second step in the control law, i.e., the method of computing the applied control torque signals from the commanded acceleration signals. If the vector of actuating joint torques  $\tau$  is computed from the commanded acceleration signal under the assumption that the joint inertias are constant, then we obtain an independent joint control scheme. On the other hand, if the actuating torques  $\tau$  are computed from the *inverse dynamics* model in equation (1) then we obtain the computed-torque scheme.

We have implemented computed-torque and the independent joint control schemes and

compared their real-time performance as a function of the sampling rate. These schemes are described in the sequel.

### 2.1. Independent Joint Control (IJC)

In this scheme, linear PD control laws were designed for each joint based on the assumption that the joints are decoupled and linear. The control torque  $r$  applied to the joints at each sampling instant is:

$$r = Ju_t \quad (5)$$

where  $J$  is the constant  $N \times N$  diagonal matrix of link inertias at a typical position.

### 2.2. Computed-Torque Control (CT)

This scheme uses nonlinear feedback to decouple the manipulator. The control torque  $r$  is computed by the inverse dynamics equation in (1), using the commanded acceleration  $u^{\wedge}$  instead of the measured acceleration  $\ddot{\theta}$ :

$$r = B(\theta)u_t + K(\theta, \dot{\theta}) + \tilde{g}(\theta) \quad (6)$$

where the " $\sim$ " indicates that the estimated values of the dynamics parameters are used in the computation.

The real-time control experiments using these schemes have been performed with the CMU DD Arm II. Also, we have used equation 4 to compute the accelerations for both the computed-torque and the independent joint control schemes. Before proceeding with the design of the controller gain matrices, we need to determine the order and transfer function of the individual joint drive systems. We achieved this by performing frequency response experiments. The details of these experiments are presented [9, 6].

## 3. Controller Design

The performance of the nonlinear CT scheme and the linear IJC scheme can be compared only if the same criteria are used for design of the controller gain matrices. Fortunately, this is possible because the gain matrices  $K_p$  and  $K_v$  appear only in the commanded accelerations which are the same (equations (2)-(4)) for both CT and IJC schemes. Thus, whether we implement the simplistic independent joint control scheme or the sophisticated computed-torque scheme, we are faced with the problem of designing the gain matrices  $K_p$  and  $K_v$ . These matrices are chosen to satisfy the specified output response criterion.

### 3.1. Design of Gain Matrices for Independent Joint Control

The closed loop transfer function relating the input  $u^{\wedge}$  to the measured output  $\theta_j$  for joint  $j$  is:

$$\frac{\delta}{\theta_{jd}} = \frac{s^2 \delta + s \gamma k_{vj} + k_{pj}}{s^2 + k_{vj} s + k_{pj}} \quad (7)$$

where  $\gamma=1$  if velocity feedforward is included and zero otherwise, and  $\delta=1$  if acceleration feedforward is included and zero otherwise. The closed-loop characteristic equation in all the three cases is,

$$s^2 + k_{vj}s + k_{pj} = 0 \quad (8)$$

and its roots are specified to obtain a stable response. The complete closed-loop response of the system is governed by both the zeros and the poles of the system. In the absence of any feedforward terms, the response is governed by the poles of the transfer function.

Since it is desired that none of the joints overshoot the commanded position or the response be critically damped, our choice of the matrices  $K_p$  and  $K_v$  must be such that their elements satisfy the condition:

$$k_{vj} = 2\sqrt{k_{pj}} \quad \text{for } j = 1, \dots, 6 \quad (9)$$

Besides, in order to achieve a high disturbance rejection ratio or high stiffness it is also necessary to choose the position gain matrix  $K_p$  as large as possible which results in a large  $K_v$ .

### 3.2. Design of Gain Matrices for Computed-Torque Scheme

The basic idea behind the computed-torque scheme is to achieve dynamic decoupling of all the joints using nonlinear feedback. If the dynamic model of the manipulator is described by equation (1) and the applied control torque is computed according to equation (6), then the following closed-loop system is obtained:

$$\ddot{\theta} = u_i - [\mathring{D}]^{-1} \{ [D - \mathring{D}]\ddot{\theta} + [h - \mathring{h}] + [g - \mathring{g}] \}$$

where the functional dependencies on  $\theta$  and  $\dot{\theta}$  have been omitted for the sake of clarity. If the dynamics are modeled exactly, that is,  $\mathring{D}=D$ ,  $\mathring{h}=h$  and  $\mathring{g}=g$ , then the decoupled closed loop system is described by

$$\ddot{\theta} = u_i$$

Upon substituting the right hand side of either (2), (3) or (4) in the above equation, we obtain the closed-loop input-output transfer function of the system. The closed-loop characteristic equation in all the three cases is:

$$s^2 + k_{vj}s + k_{pj} = 0 \quad (10)$$

where  $k_{vj}$  and  $k_{pj}$  are the velocity and position gains for the  $j$ -th joint. Upon comparing equations (8) and (10), we obtain the relationships

$$k_{pj}^{[CT]} = k_{pj}^{[IJC]} \quad \text{and} \quad k_{vj}^{[CT]} = k_{vj}^{[IJC]}$$

which suggest that the gains of the IJC scheme are also the gains of the CT scheme. This

equality must be expected because the closed-loop characteristic equation for both the independent joint control and the computed-torque scheme is the same.

### 3.3. Gain Selection

The gain matrices  $K_p$  and  $K_v$  are a function of the sampling rate of the control system [3]. The higher the sampling rate the larger the values of  $K_p$  and  $K_v$  can be chosen. Since the stiffness (or disturbance rejection property) of the system is governed by the position gain matrix a higher sampling rate implies higher stiffness also. In practice the choice of the velocity gain  $K_v$  is limited by the noise present in the velocity measurement. We determined the upper limit of the velocity gain experimentally: we set the position gain to zero and increased the velocity gain of each joint until the unmodeled high-frequency dynamics of the system were excited by the noise introduced in the velocity measurement. This value of  $K_v$  represents the maximum allowable velocity gain. We chose 80% of the maximum velocity gain in order to obtain as high value of the position gain as possible and still be well within the stability limits with respect to the unmodeled high frequency dynamics. The elements of the position gain matrix  $K_p$  were computed to satisfy the critical damping condition in (9) and also achieved the maximum disturbance rejection ratio. The elements of the velocity and position gain matrices used in the implementation of the control schemes are listed in Table 1.

## 4. Experiments and Results

### 4.1. Trajectory Selection and Evaluation Criteria

Since the DD Arm II is a highly nonlinear and coupled system it is impossible to characterize its behavior from a particular class of inputs, unlike linear systems for which a specific input (such as a unit step or a ramp) can be used to design and evaluate the controllers. Thus an important constituent of the experimental evaluation of robot control schemes is the choice of a class of inputs for the robot. The criteria for selecting the joint trajectories is detailed by Khosla [6]. For evaluating the performance of robot control schemes, we use the dynamic tracking accuracy. This is defined as the maximum position and velocity tracking error along a specified trajectory.

### 4.2. Real-Time Results

In our experiments we implemented both the independent joint control scheme and the computed-torque scheme. We evaluated their individual and relative performances by changing the sampling rate but keeping both the position and the velocity gain matrices fixed. The maximum permissible velocity and position gains were chosen at a control sampling period of 5 ms (according to the method outlined in Section 3.3) and remained fixed even when the sampling period was changed. This allows us to determine the effect of the sampling rate on the trajectory tracking control performance. We have also evaluated the best performance of the CT method for a sampling period of 2 ms with its best performance for a sampling period of 5 ms. We conducted the evaluation experiments on a multitude of trajectories but due to space limitations we present our results for a

simple but illustrative trajectory.

The first trajectory is chosen to be simple and relatively slow but capable of providing insight into the effect of dynamics compensation. In this trajectory only joint 2 moves while all the other joints are commanded to hold their zero positions and can be envisioned from the schematic diagram in Figure 1. Joint 2 is commanded to start from its zero position and to reach the position of L5 rad in 0.75 seconds; it remains at this position for an interval of 0.75 seconds after which it is required to return to its home position in 0.75 seconds. The points of discontinuity, in the trajectory, were joined by a fifth-order polynomial to maintain the continuity of position, velocity and acceleration along the three segments. The desired position, velocity and acceleration trajectories for joint 2 are depicted in Figure 2. The maximum velocity and acceleration to be attained by joint 2 are 2 rad/sec and 6 rad/sec<sup>2</sup>, respectively.

The position tracking performance of joint 2 for both the CT and IJC schemes, for a control sampling rate of 200 Hz (corresponding to a control sampling period of 5 ms), is depicted in Figure 3. The corresponding position and velocity tracking errors are presented in Figures 4 and 5, respectively. We also depict the position tracking error of joint 1 in Figure 6 for both the CT and IJC schemes. We note that the CT scheme outperforms the IJC scheme. For example, in the case of joint 2 the maximum position tracking error for CT scheme is 0.03 rads while for the IJC scheme it is 0.45 rads, approximately. In an earlier paper [9], we had compared both the CT and IJC schemes with a control sampling period of 2 ms. It must be noted that in the earlier reported experiments the gains were selected for a control sampling period of 2 ms whereas in the present experiments the gains have been selected for a control sampling period of 5 ms. To put the results in perspective, we recall that in the earlier experiment the maximum position tracking error for the CT method was 0.022 rads while for the IJC method it was 0.036 rads. From the above observations it may be deduced that increasing the control sampling period from 2 to 5 ms results in a noteworthy degradation of the performance of the DC scheme. A similar increase in the sampling rate also improves the performance of the CT scheme.

In Figure 7 we depict the performance of the CT scheme as the sampling rate is increased from 200 Hz to 500 Hz. In this case the position and velocity gain matrices were determined for a sampling rate of 200 Hz and they remained fixed even when the sampling rate was increased to 500 Hz. Thus, in Figure 7 we present the relative performance of the CT method as a function of the sampling rate only. We note that the trajectory tracking performance for both 200 Hz and 500 Hz sampling rate is comparable and has not changed in any appreciable manner with an increase in the sampling rate. Figure 8 depicts the results for the IJC method when a similar experiment was performed. In this case also we do not observe any appreciable change in performance when only the sampling rate is changed.

Thus, from the above set of experiments the following conclusions may be drawn:

1. The gains are selected for a lower sampling rate and then if the sampling rate

is increased, while keeping the gains fixed, there is no appreciable improvement in the performance of both the CT and the IJC schemes.

2. At lower sampling rates the CT scheme outperforms the IJC method. Even though the disturbance rejection ratio of both the schemes is diminished, it does not appreciably affect the CT method because of the compensation for the nonlinear and coupling terms. It affects the IJC method, however, because the disturbance that is constituted by the nonlinear and the coupling terms is not rejected appreciably.
3. If the maximum possible gains are selected for the chosen sampling rates, then the performance of CT at a higher sampling rate is better than its performance at a lower sampling rate. A similar conclusion is drawn for the IJC scheme also.

Our last conclusion is especially significant because it suggests that a higher sampling rate does not only imply improved performance, but it also allows us to achieve high stiffness. It is desirable for a manipulator to have high stiffness so that the effect of unpredictable external disturbances on the trajectory tracking performance is significantly reduced.

## 5. Summary

In this paper, we have presented the first experimental evaluation of the effect of the sampling rate on the performance of both the computed-torque and the independent joint control schemes. We have discussed the design of the controller gains for both the independent joint control and the computed-torque schemes and established a framework for the comparison of their trajectory tracking performance. Based on our experiments we have demonstrated that the computed-torque scheme exhibits a better performance than the independent joint control scheme. Our experiments also show that high sampling rates are important because they result in a stiffer system that is capable of effectively rejecting unknown external disturbances.

## 6. Acknowledgements

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## I. The CMU DD Arm II

We have developed, at CMU, the concept of direct-drive robots in which the links are directly coupled to the motor shaft. This construction eliminates undesirable properties like friction and gear backlash. The CMU DD Arm II [14] is the second version of the CMU direct-drive manipulator and is designed to be faster, lighter and more accurate than its predecessor CMU DD Arm I [2]. We have used brushless rare-earth magnet DC torque

motors driven by current controlled amplifiers to achieve a torque controlled joint drive system. The SCARA-type configuration of the arm reduces the torque requirements of the first two joints and also simplifies the dynamic model of the arm. To achieve the desired accuracy, we use very high precision (16 bits/rotation) rotary absolute encoders. The arm weighs approximately 70 pounds and is designed to achieve maximum joint accelerations of  $10 \text{ rad/sec}^2$ .

The hardware of the DD Arm II control system consists of three integral components: the Motorola M68000 microcomputer, the Marince processor and the TMS-320 microprocessor-based individual joint controllers. We have also developed the customized Newton-Euler equations for the CMU DD Arm II and achieved a computation time of  $1 \text{ ms}$  by implementing these on the Marince processor. The details of the customized algorithm, hardware configuration and the numerical values of the dynamics parameters are presented in Kanade, et al. [5].

**Table 1: Transfer Functions and Gains of Individual Links**

Joint (j)	Transfer Function ( $\frac{1}{J_j s^2}$ )	$k_{pj}$	$k_{vj}$
1	$\frac{1}{12.3s^2}$	2.75	3.33
2	$\frac{1}{2s^2}$	15.0	7.5
3	$\frac{1}{0.25s^2}$	256.0	32.0
4	$\frac{1}{0.007s^2}$	1285.0	71.5
5	$\frac{1}{0.006s^2}$	625.0	50.0
6	$\frac{1}{0.0003s^2}$	1110.0	50.0

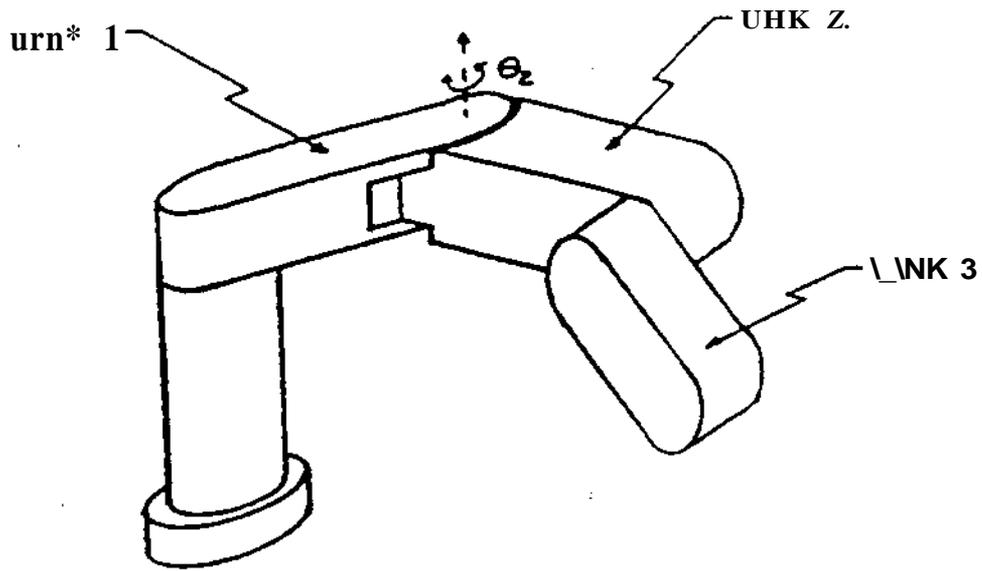


Figure 1: Schematic diagram of 3 DOF DD Ann II

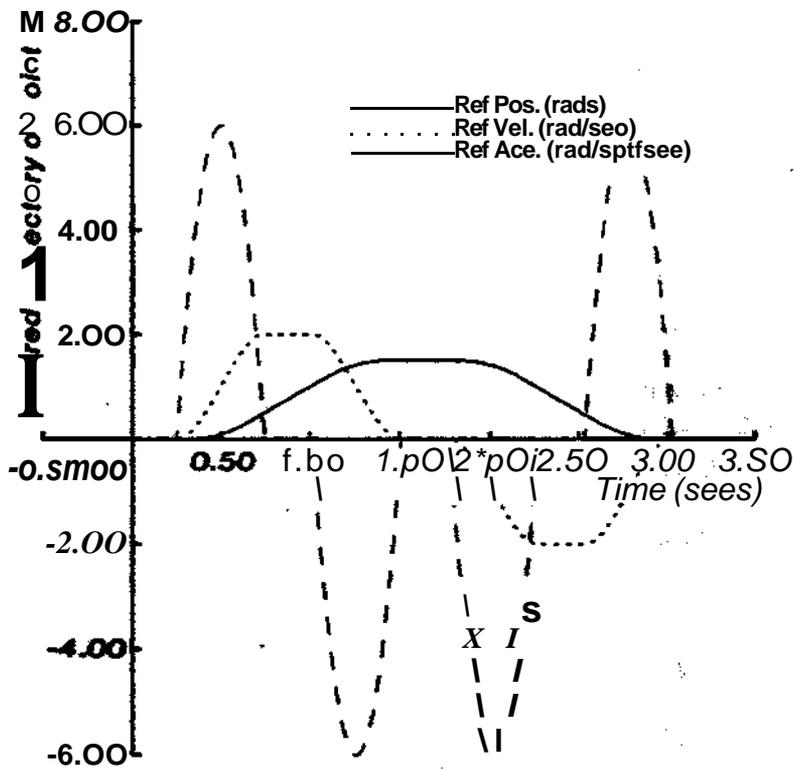


Figure 2; Desired trajectories for joint 2

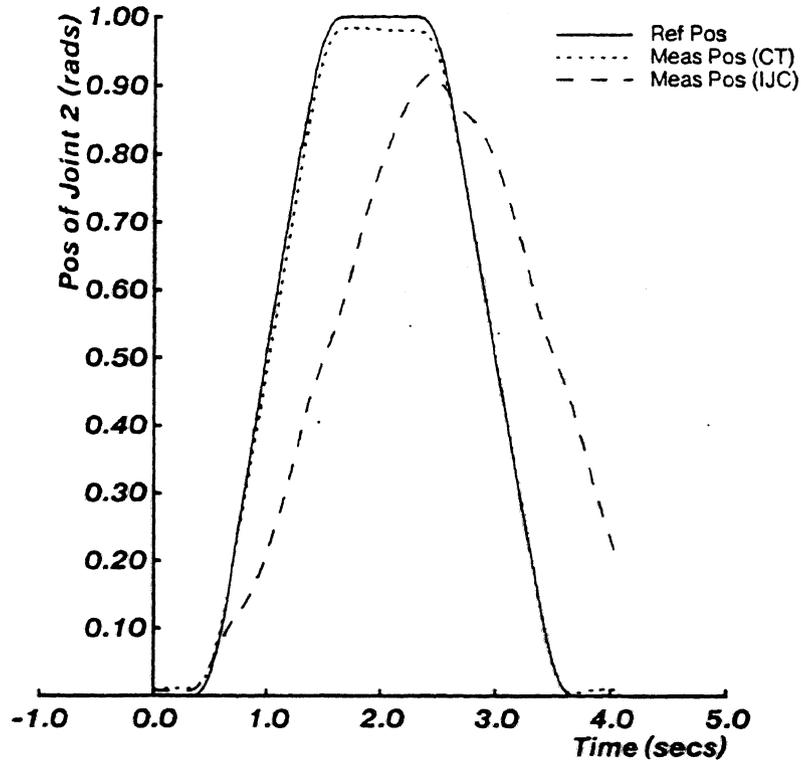


Figure 3: Position tracking of CT and IJC at 5 ms sampling

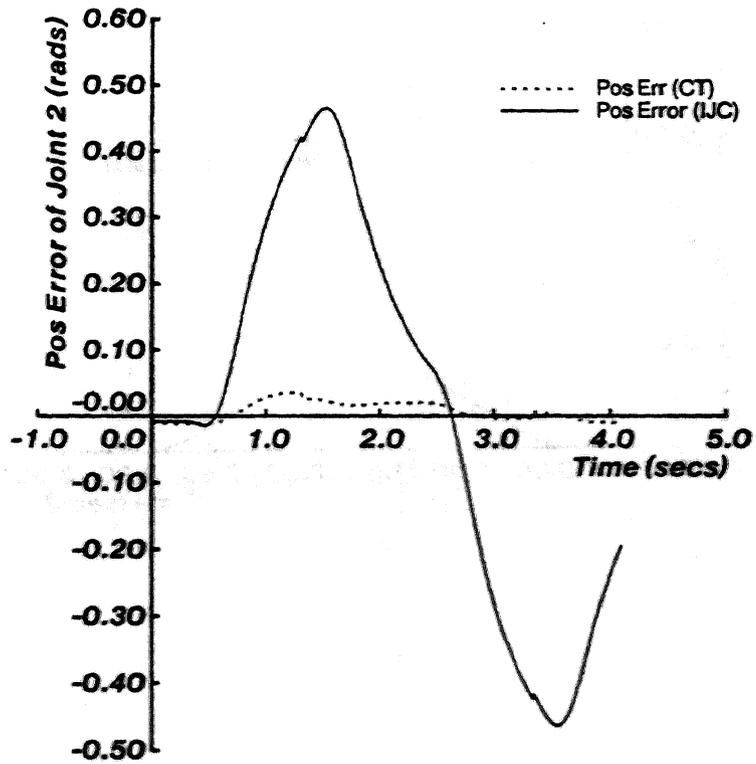


Figure 4: Position tracking error of joint 2

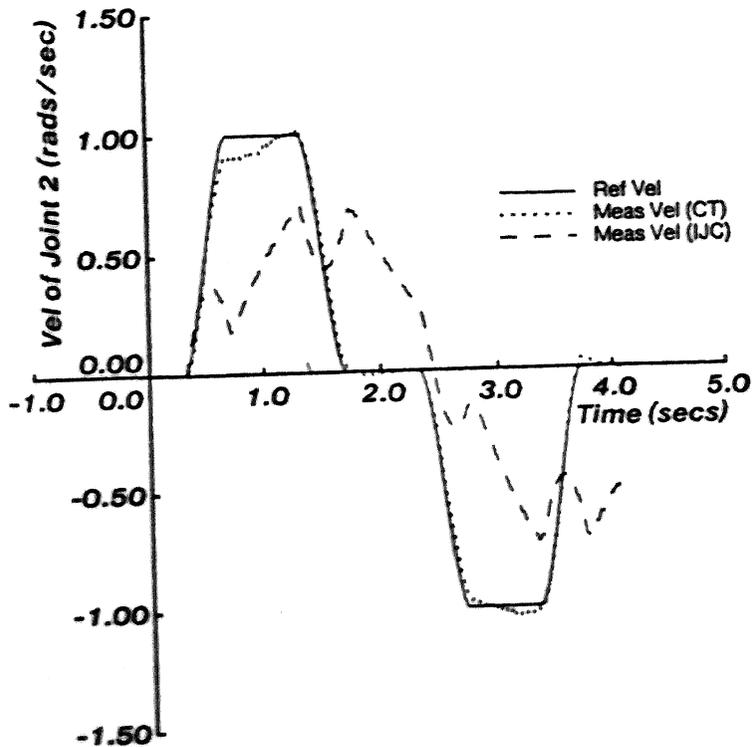


Figure 5: Velocity tracking errors of joint 2

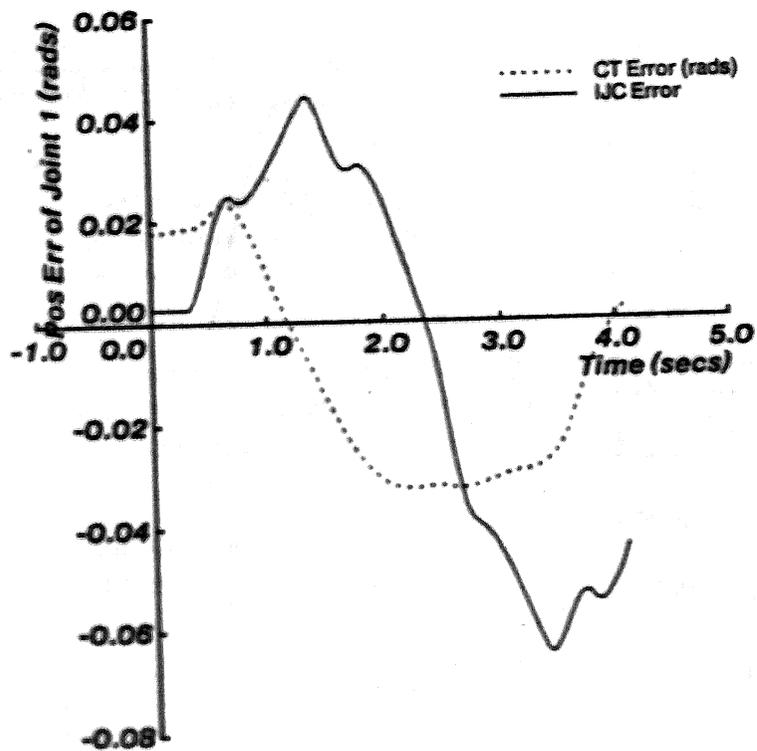


Figure 6: Position tracking errors of joint 1

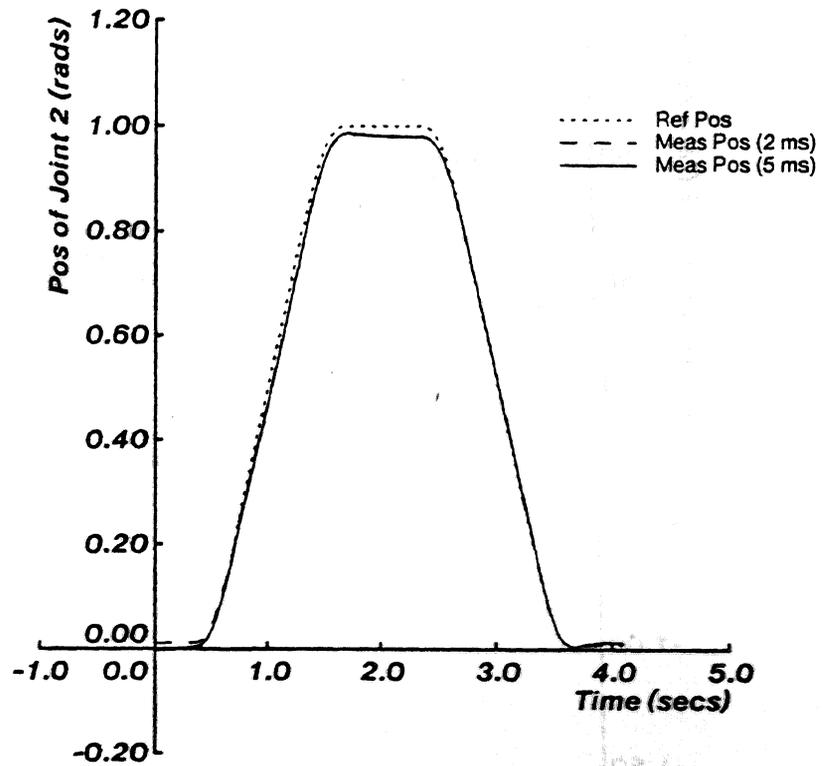


Figure 7: Performance of CT as a function of sampling period

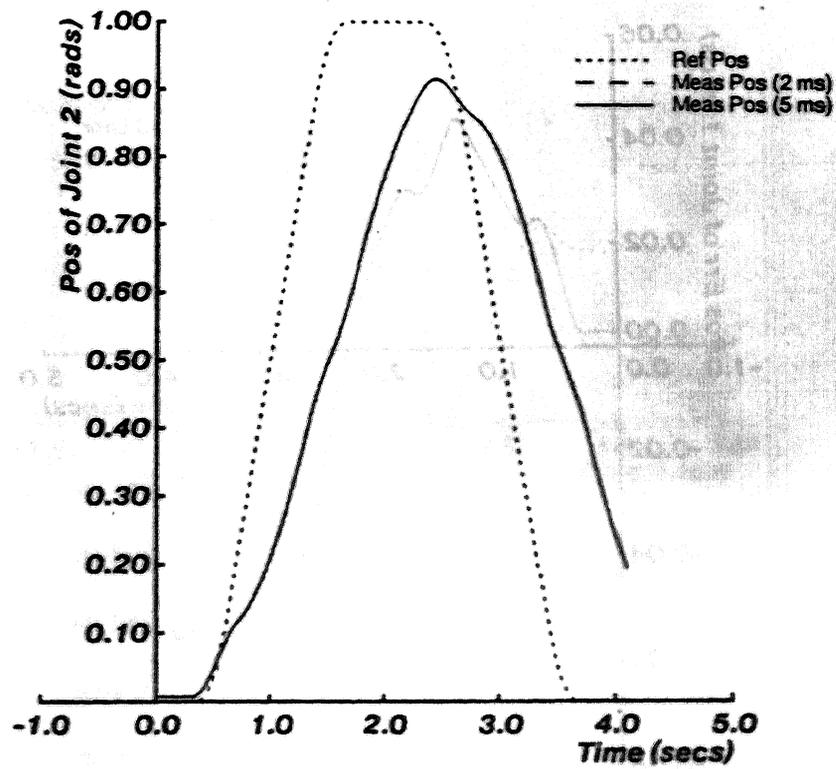


Figure 8: Performance of IJC as a function of sampling period

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