

By (2.27) we have in a similar fashion, $t_{r'j} = t_{r'r'}$, and $t_{s'j} = t_{s's'}$.

By Remark 5, we have on a C^r -boundary

$$t_{r'j} = t_{rj} = t = t_{rr}, t_{r'r} = t_{sf}, t_{s'j} = t_{sf}, t_{ss} = t_{s's'} \quad (3.17)$$

On a C^r -boundary $t_* = t_s = t_{s'} = t_{r'}$. Let C be a smooth portion of a C^1 -boundary having proper slope. We parameterize C in the (r,s) plane by $(h(J), k(J))$ and c' in the (r',s') plane by $(\bar{h}(f), \bar{k}(f))$. Then

$$t_{r'f} = h' t_{rr} + k' t_{rs}$$

$$t_{s'f} = \bar{h}' t_{sr} + \bar{k}' t_{ss}$$

By (2.24) and the fact that $t_r = t_s$, $t_{rs} = 0$ on C .

Thus, on C $t_{r'f} = h' t_{rr}$ and $t_{s'f} = k' t_{ss}$.

Similarly on c' $t_{r'f} = \bar{h}' t_{rr}$ and $t_{s'f} = \bar{k}' t_{ss}$.

Since on C $t_r = t_s = t_{s'} = t_{r'}$, we have $t_{r'j} = t_{s'j} = t_{s'k} = t_{r'j}$.

Select J so that $h'(J) > 0$, then on the C^* -boundary C and C^* , since C has proper slope,

$$\text{sgn}(t_{r'f}) = \text{sgn}(t_{rj}) = \text{sgn}(t_{s'f}) = \text{sgn}(t_{s'j}) = \text{sgn}(t_{ss}) = \text{sgn}(t_{s'k}) = \text{sgn}(t_{r'j})$$

for C with positive slope,

(3.18)

$$\text{sgn}(t_{r'f}) = \text{sgn}(t_{rr}) = \text{sgn}(-t_{sg}) = \text{sgn}(t_{r'f}) = \text{sgn}(-t_{g/g'}) = \text{sgn}(t_{r'f})$$

for C with negative slope.

By (1.101) the condition $f = 0$ or $f_{tt} = 0$ is necessary in order for a curve to be an internal boundary. We now investigate the extent to which this is sufficient. A curve is an internal boundary if it separates plastic